

Problems 38 and 39 on page 209.

Find the power series solution of each of the following. Give the interval of convergence of each.

1.  $y'' + xy' + y = 0$ ,  $y(0) = 1$ ,  $y'(0) = 0$ .
2.  $y'' + xy' + y = 0$ ,  $y(0) = 0$ ,  $y'(0) = 1$ .
3.  $(1 - x)y'' + y = 0$ ,  $y(0) = 0$ ,  $y'(0) = 1$ ,
4.  $(1 - x)y'' + y = 0$ ,  $y(0) = 1$ ,  $y'(0) = 0$ ,
5.  $y'' + xy' + 2y = 0$ .
6.  $(1 + x^2)y'' - 4xy' + 6y = 0$ .